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**DEPT : B E COMPUTER SCIENCE AND ENGINEERING - B**

# Dynamic Programming

* 1. **Playing with Numbers**

**Aim:** Ram and Sita are playing with numbers by giving puzzles to each other. Now it was Ram term, so he gave Sita a positive integer ‘n’ and two numbers 1 and 3. He asked her to ﬁnd the possible ways by which the number n can be represented using 1 and 3.Write any eﬃcient algorithm to ﬁnd the possible ways.

Example 1:

*Input: 6 Output:*

*6*

*Explanation: There are 6 ways to 6 represent number with 1 and 3*

*1+1+1+1+1+1*

*3+3*

*1+1+1+3*

*1+1+3+1*

*1+3+1+1*

*3+1+1+1*

Input Format

First Line contains the number n

Output Format

Print: The number of possible ways ‘n’ can be represented using 1 and 3 Sample Input

6

Sample Output 6

## Algorithm:

function countWays(n)

{

initialize a of size n + 1 // Array to store the number of ways

a[0] = 1 // Base case: 1 way to climb 0 stairs a[1] = 1 // Base case: 1 way to climb 1 stair

if n >= 2

{

a[2] = 1 // Base case: 1 way to climb 2 stairs

}

if n >= 3

{

a[3] = 2 // Base case: 2 ways to climb 3 stairs

}

// Fill the array for all stairs from 4 to n for i from 4 to n

{

a[i] = a[i - 1] + a[i - 3] // Total ways to climb i stairs

}

return a[n] // Return the number of ways to climb n stairs

}

function main()

{

initialize n // Number of stairs read n from user

result = countWays(n) // Calculate the number of ways print result // Print the result

return 0

}

## Program:

#include <stdio.h>

long long int countWays(int n)

{ long long int a[n + 1];

a[0] = 1;

a[1] = 1;

if (n >= 2) {

a[2] = 1;

}

if (n >= 3) {

a[3] = 2;

}

for (int i = 4; i <= n; i++) {

a[i] = a[i - 1] + a[i - 3];

}

return a[n];

}

int main()

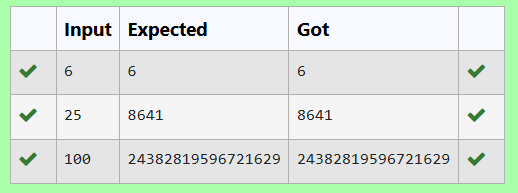
{ int n; scanf("%d", &n);

long long int result = countWays(n); printf("%lld",result);

return 0;

}

**Output:**



# Playing with chessboard

**Aim:** Ram is given with an n\*n chessboard with each cell with a monetary value. Ram stands at the (0,0), that the position of the top left white rook. He is been given a task to reach the bottom right black rook position (n-1, n-1) constrained that he needs to reach the position by traveling the maximum monetary path under the condition that he can only travel one step right or one step down the board. Help ram to achieve it by providing an efficient DP algorithm.

Example:

Inpu t 3

1 2 4

2 3 4

8 7 1

Output:

19

Explanation:

Totally there will be 6 paths among that the optimal is Optimal path value:1+2+8+7+1=19

Input Format

First Line contains the integer n

The next n lines contain the n\*n chessboard values Output Format

Print Maximum monetary value of the path

**Algorithm:**

function max(a, b)

{

return (a > b) ? a : b // Return the maximum of a and b

}

function maxMonetaryPath(n, board)

{

initialize dp[n][n] // Array to store maximum monetary path sums

dp[0][0] = board[0][0] // Starting point

// Fill the ﬁrst row for j from 1 to n - 1

{

dp[0][j] = dp[0][j - 1] + board[0][j]

}

// Fill the ﬁrst column for i from 1 to n - 1

{

dp[i][0] = dp[i - 1][0] + board[i][0]

}

// Fill the rest of the dp table for i from 1 to n - 1

{

for j from 1 to n - 1

{

dp[i][j] = board[i][j] + max(dp[i - 1][j], dp[i][j - 1])

}

}

return dp[n - 1][n - 1] // Return the maximum monetary path to the bottom-right corner

}

function main()

{

initialize n // Size of the board read n from user

initialize board[n][n] // Create the board array for i from 0 to n - 1

{

for j from 0 to n - 1

{

read board[i][j] from user

}

}

result = maxMonetaryPath(n, board) // Calculate the maximum monetary path print result // Print the result

}

## Program:

#include <stdio.h>

int max(int a, int b) { return (a > b) ? a : b;

}

int maxMonetaryPath(int n, int board[n][n])

{ int dp[n][n];

dp[0][0] = board[0][0];

for (int j = 1; j < n; j++) {

dp[0][j] = dp[0][j - 1] + board[0][j];

}

for (int i = 1; i < n; i++) {

dp[i][0] = dp[i - 1][0] + board[i][0];

}

for (int i = 1; i < n; i++) { for (int j = 1; j < n; j++) {

dp[i][j] = board[i][j] + max(dp[i - 1][j], dp[i][j - 1]);

}

}

return dp[n - 1][n - 1];

}

int main()

{ int n; scanf("%d", &n);

int board[n][n];

for (int i = 0; i < n; i++) { for (int j = 0; j < n; j++)

{

scanf("%d", &board[i][j]);

}

}

int result = maxMonetaryPath(n, board); printf("%d\n", result);

}

**Output:**



# Longest Common Subsequence

**Aim:** Given two strings ﬁnd the length of the common longest subsequence(need not be contiguous) between the two.

Example:

s1:

ggtabe s2:

tgatasb

s1 a g

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| **g** | **t** | **a** |  | |
| **t** | x | **a** | y | **b** |

s2 **g** x

The length is 4

Solveing it using Dynamic Programming

For example:

|  |  |
| --- | --- |
| **Input** | **Result** |
| aab  azb | 2 |

**Algorithm:**

int longestCommonSubsequence(s1, s2)

{

m = length of s1 // Length of ﬁrst string

n = length of s2 // Length of second string

initialize dp[m + 1][n + 1] // DP table

// Initialize the DP table with base cases for i from 0 to m

{

for j from 0 to n

{

if i == 0 or j == 0

{

dp[i][j] = 0 // Base case: LCS of an empty string

}

else if s1[i - 1] == s2[j - 1]

{

dp[i][j] = dp[i - 1][j - 1] + 1 // Characters match

}

else

{

dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]) // Characters do not match

}

}

}

return dp[m][n] // Return length of LCS

}

function main()

{

initialize s1[100], s2[100] // Arrays to hold the strings

read s1 from user read s2 from user

result = longestCommonSubsequence(s1, s2) // Calculate LCS print result // Print the result

}

**Program:**

#include

<stdio.h> #include

<string.h>

int longestCommonSubsequence(char s1[], char s2[]) { int m = strlen(s1);

int n = strlen(s2);

int dp[m + 1][n + 1];

// Initialize the DP table with base cases for (int i = 0; i <= m; i++) {

for (int j = 0; j <= n; j++)

{ if (i == 0 || j == 0) { dp[i][j] = 0;

}

else if (s1[i - 1] == s2[j - 1]) {

dp[i][j] = dp[i - 1][j - 1] + 1;

}

else {

dp[i][j] = (dp[i - 1][j] > dp[i][j - 1]) ? dp[i - 1][j] : dp[i][j - 1];

}

}

}

return dp[m][n];

}

int main() {

char s1[100], s2[100];

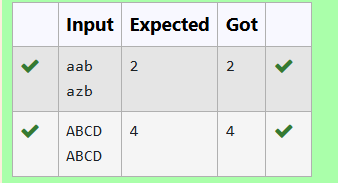
scanf("%s", s1);

scanf("%s", s2);

int result = longestCommonSubsequence(s1, s2); printf("%d", result);

}

**Output:**



# Longest non-decreasing Subsequence

**Aim:** Problem statement:

Find the length of the Longest Non-decreasing Subsequence in a given Sequence.

Eg:

Input:9

Sequence:[-1,3,4,5,2,2,2,2,3]

the subsequence is [-1,2,2,2,2,3] Output:6

## Algorithm:

int longestNonDecreasingSubsequence(n, sequence)

{

initialize dp[n] // Array to hold the lengths of subsequences maxLength = 1 // Initialize the maximum length

// Initialize dp array where each element is 1 for i from 0 to n - 1

{

dp[i] = 1

}

// Calculate the length of the longest non-decreasing subsequence for i from 1 to n - 1

{

for j from 0 to i - 1

{

if sequence[j] <= sequence[i]

{

dp[i] = max(dp[i], dp[j] + 1) // Update dp[i] if a longer subsequence is found

}

}

maxLength = max(maxLength, dp[i]) // Update the maximum length found

}

return maxLength // Return the length of the longest non-decreasing subsequence

}

function main()

{

initialize n // Number of elements in the sequence read n from user

initialize sequence[n] // Array to hold the sequence

// Read values into the sequence for i from 0 to n - 1

{

read sequence[i] from user

}

result = longestNonDecreasingSubsequence(n, sequence) // Calculate result print result // Print the result

}

## Program:

#include <stdio.h>

int longestNonDecreasingSubsequence(int n, int sequence[])

{ int dp[n];

int maxLength = 1;

for (int i = 0; i < n; i++) { dp[i] = 1;

}

for (int i = 1; i < n; i++) { for (int j = 0; j < i; j++)

{

if (sequence[j] <= sequence[i]) {

dp[i] = (dp[i] > dp[j] + 1) ? dp[i] : dp[j] + 1;

}

}

maxLength = (maxLength > dp[i]) ? maxLength : dp[i];

}

return maxLength;

}

int main()

{ int n; scanf("%d", &n);

int sequence[n];

for (int i = 0; i < n; i++) { scanf("%d", &sequence[i]);

}

int result = longestNonDecreasingSubsequence(n, sequence); printf("%d", result);

}

## Output:

